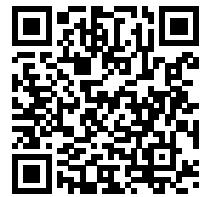


Worksheet: L01 – Symbolic Reasoning

CSCI-534: Robot Planning & Manipulation

Spring 2020

<http://www.neil.dantam.name/rpm/B01-sym.pdf>



1. S-expressions:

(a) For expression $2(x - 1) = 4$:

i. Draw the equivalent abstract syntax tree:

ii. Write the equivalent S-expression:

iii. Draw the equivalent cons cell diagram.

(b) For expression $a + bx + cx^2$:

i. Draw the equivalent abstract syntax tree:

ii. Write the equivalent S-expression:

iii. Draw the equivalent cons cell diagram.

2. List construction: evaluate the following:

- (a) (cons 'x 'y)
- (b) (cons 'x '(y z))
- (c) (cons 'x (list 'y 'z))
- (d) (list (+ 1 2 3))
- (e) (list' (+ 1 2 3))
- (f) (list' * (+ 2 2)'(- 2 2))
- (g) (list' + '(* a 2) (* 3 4))

3. List templates: Evaluate the following list templates:

- (a) '(1 2 ,(+ 3 4))
- (b) '(,1 ,2 (+ 3 4))
- (c) '(+ 1 ,2 ,(+ 3 4))
- (d) '(1 2 ,@(list '+ '3 '4))

4. Recursive Evaluation: For expression $2(1 + 2 + 3) - 5$:

- (a) Draw the equivalent abstract syntax tree:
- (b) Write the equivalent S-expression:
- (c) Show the steps of the recursive evaluation diagram:

5. **Partial Evaluation:** show the partial evaluation steps for $e = \frac{a}{1+b+c} - d$, where $a = 3$, $b = 5$, and $c = 7$:

6. **Derivative s-expression:** For expression $\frac{d}{dt} \frac{\sin t}{\cos t}$:

(a) Write the equivalent s-expression:

(b) Draw the equivalent cons cell diagram:

7. **Differential calculus s-expression:** Write the following differential calculus rules in S-expression form:

$$(a) \frac{d}{dt} (f(t) - g(t)) \rightsquigarrow \frac{d}{dt} f(t) - \frac{d}{dt} g(t)$$

$$(b) \frac{d}{dt} \left(\frac{f(t)}{g(t)} \right) \rightsquigarrow \frac{\frac{d}{dt} f(t)}{g(t)} - \frac{f(t) * \frac{d}{dt} g(t)}{(g(t))^2}$$

8. **Symbolic differentiation:** Trace the steps of the recursive symbolic differentiation algorithm for the following expressions:

(a) $\frac{d}{dt} \sin^2 t$

(b) $\frac{d}{dx} (\ln x + a * x^2)$